

Greenfields Progression of Calculation in Mathematics Policy

1 Aims and objectives

1.1 Mathematics at Greenfields provides a structured and systematic approach to the teaching of calculation, with considerable emphasis on following a Concrete-Pictorial-Abstract approach. We believe this enables children to build a deep understanding of concepts and effective mental calculation abilities.

At Greenfields we believe a consistent approach to the teaching of written calculations is needed to establish continuity and progression throughout the school.

The aims of Calculation in mathematics are:

- For all children to be able to choose an efficient method; mental, written or calculator, appropriate to the given task.**
- For all children to have been taught, and be secure with, a standard method for each operation, with most children using the compact method by the end of Key Stage 2.**
- For all children by the end of Year 6 to be working in line with National expectations**

2 Progression of Calculation

Children will progress through calculation as follows:

- Use age-appropriate methods and resources to support conceptual understanding (see below for year group progression)**
- Establish mental methods based on a good understanding of place value.**
- Use of informal jottings to aid mental calculations.**

- Develop use of an empty number line to aid mental imagery and recording.
- Use of partitioning to aid informal methods.
- Use of expanded written methods.
- Develop use of expanded written methods into compact standard written form.

2.2 Before carrying out a calculation, children will be encouraged to consider:

- Can they do it in their head? (Using rounding, adjustment)
- The size of the approximate answer (estimation)
- Could I do jottings to keep track of the calculation?
- Do I need to use an expanded or compact written method?

3 Written Calculations

3.1 All children will work through a progression for each of the four areas of calculation, multiplication, division, addition and subtraction. This progression for calculation has been updated and agreed by staff in **Autumn 2022**. (See below)

4 Monitoring and review

4.1 Monitoring of the standards of children's work and of the quality of teaching calculation is the responsibility of the mathematics subject leader. The work of the mathematics subject leader also involves supporting colleagues in the teaching of calculation. The mathematics subject leader gives the head teacher an annual summary in which they evaluate strengths and

weaknesses in the subject including calculation and indicates areas for further improvement. The subject leader reviews samples of children's work, planning and undertakes learning walks of mathematics teaching across the school.

5 EYFS

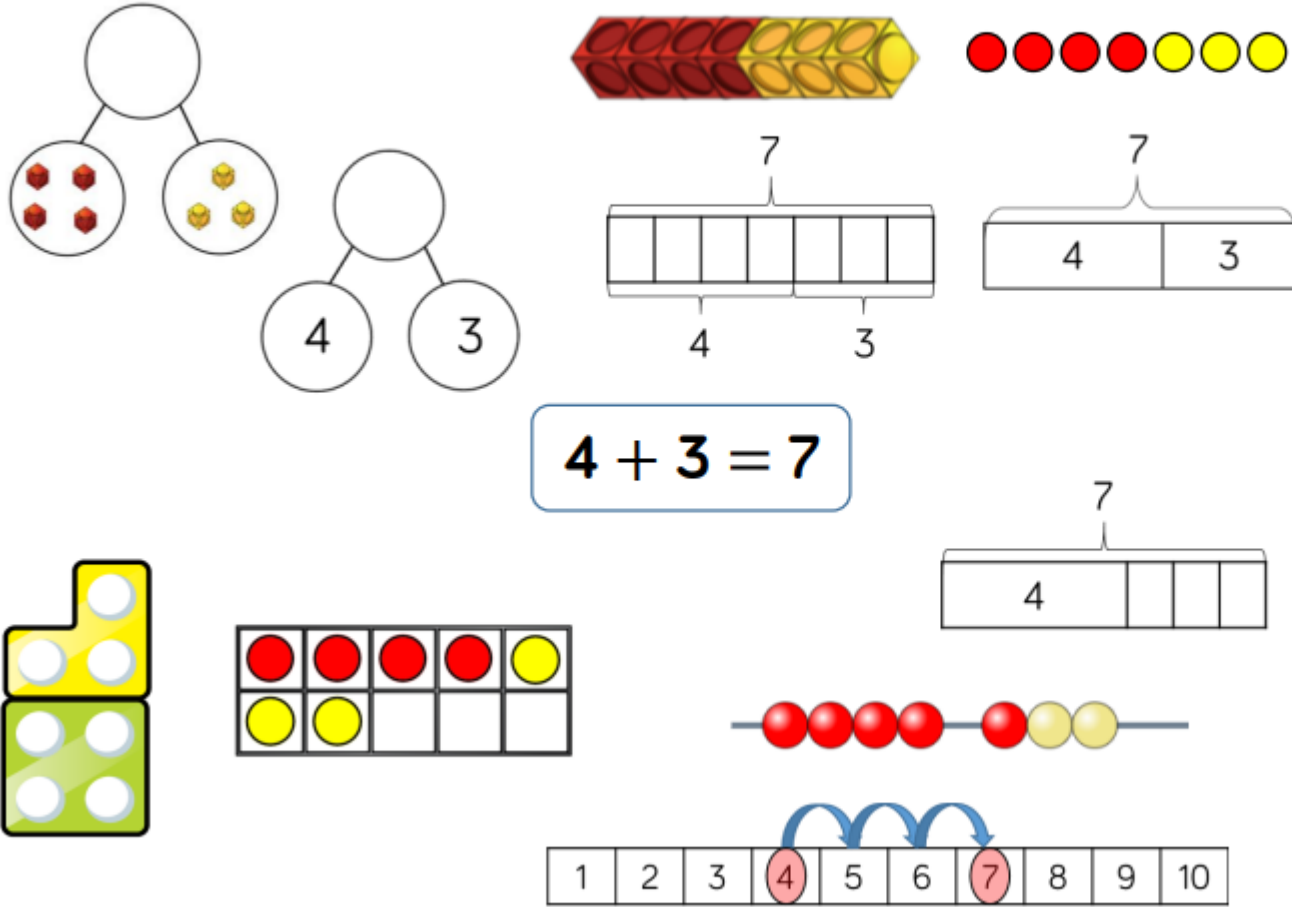
5.1 EYFS will focus on early counting, number and shape, space and measure concepts outlined in the Early Years Frame and in birth to Five Matters. Representations and models used in Year 1 will also be introduced in EYFS.

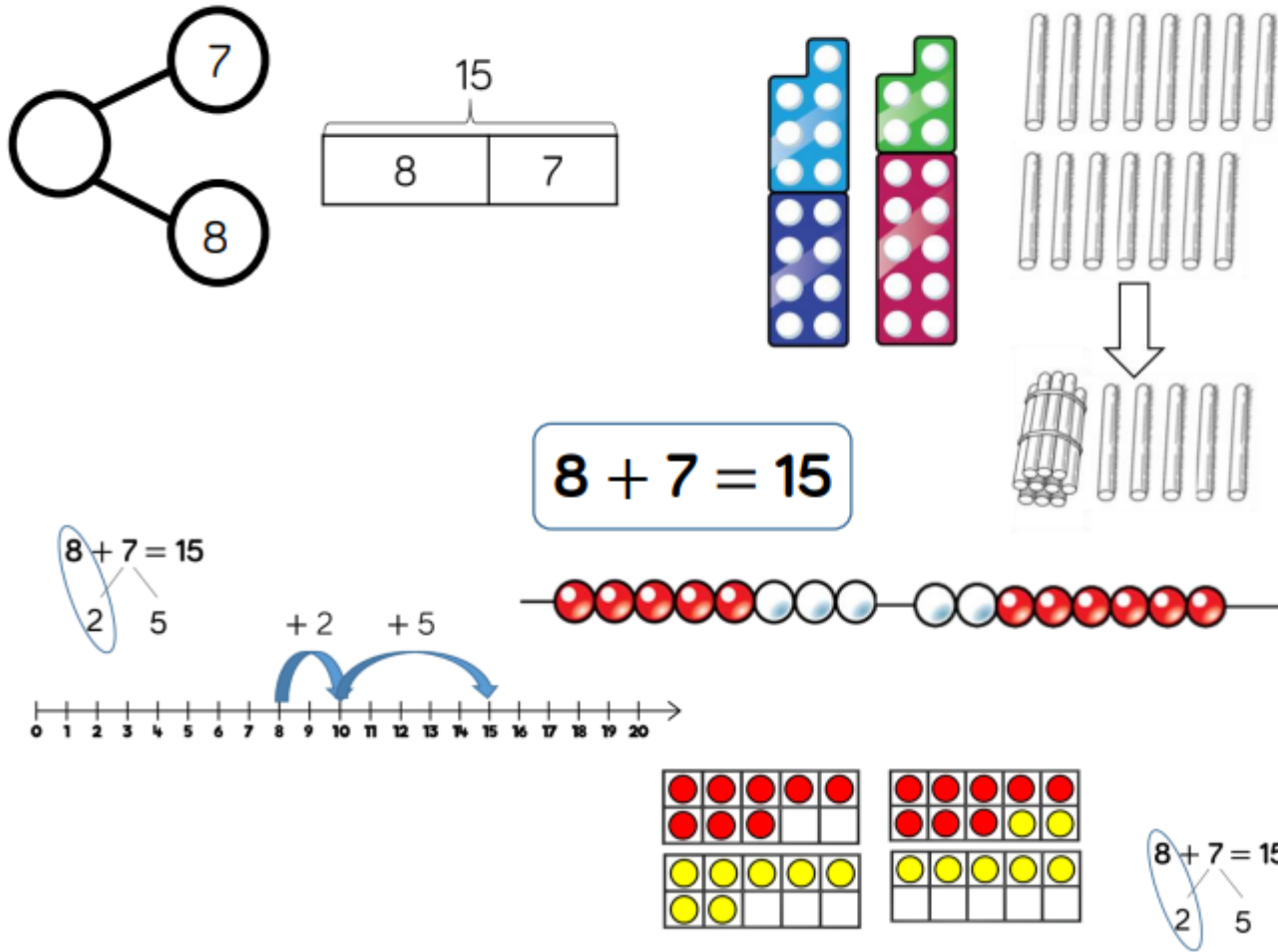
Addition

Skill	Year	Representations and models	
Add two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes	Ten frames (within 10) Bead strings (10) Number tracks
Add 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20)	Bead strings (20) Number tracks Number lines (labelled) Straws
Add three 1-digit numbers	2	Part-whole model Bar model	Ten frames (within 20) Number shapes
Add 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled)	Number lines (blank) Straws Hundred square

Progression of Calculation in Mathematics Policy

Skill	Year	Representations and models	
Add two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws	Base 10 Place value counters
Add with up to 3-digits	3	Part-whole model Bar model	Base 10 Place value counters Column addition
Add with up to 4-digits	4	Part-whole model Bar model	Base 10 Place value counters Column addition
Add with more than 4 digits	5	Part-whole model Bar model	Place value counters Column addition
Add with up to 3 decimal places	5	Part-whole model Bar model	Place value counters Column addition

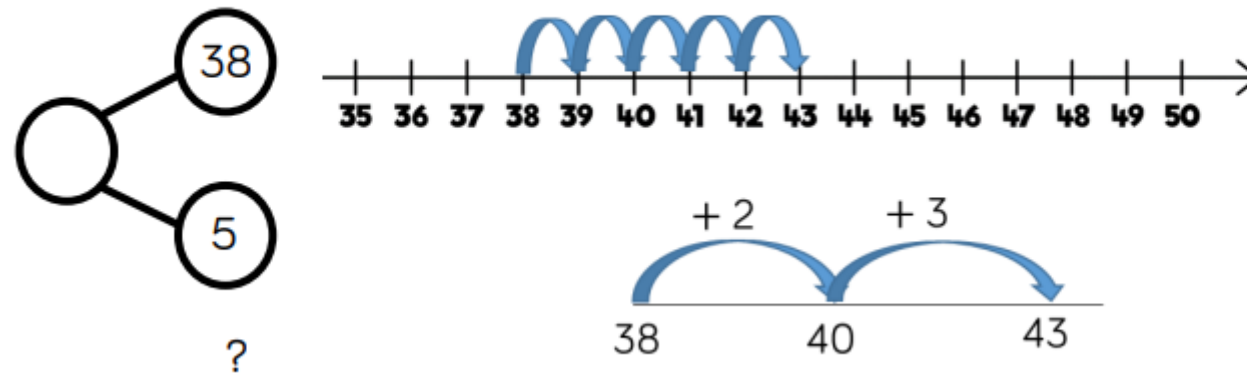
Skill: Add 1-digit numbers within 10	Year: 1
 <p>$4 + 3 = 7$</p>	<p>When adding numbers to 10, children can explore both aggregation and augmentation.</p> <p>The part-whole model, discrete and continuous bar model, number shapes and ten frame support aggregation.</p> <p>The combination bar model, ten frame, bead string and number track all support augmentation.</p>

Skill: Add 1 and 2-digit numbers to 20	Year: 1/2
 <p>$8 + 7 = 15$</p> <p>$8 + 7 = 15$</p> <p>$8 + 7 = 15$</p> <p>$8 + 7 = 15$</p>	<p>When adding one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten. In Year 1, this is only done just by counting on. From Year 2, use different manipulatives can be used to represent this exchange alongside number lines to support children in understanding how to partition their jumps.</p>

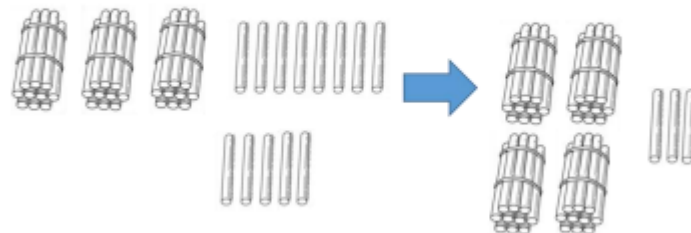
Skill: Add three 1-digit numbers	Year: 2
<div data-bbox="275 371 772 774"> </div> <div data-bbox="835 376 1525 646"> </div> <div data-bbox="801 790 1256 898"> $7 + 6 + 3 = 16$ </div> <div data-bbox="286 983 716 1217"> </div> <div data-bbox="757 1023 994 1165"> $7 + 6 + 3 = 16$ <p>10</p> </div> <div data-bbox="1072 963 1547 1283"> </div>	<p>When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add the numbers more efficiently.</p> <p>This supports children in their understanding of commutativity.</p> <p>Manipulatives that highlight number bonds to 10 are effective when adding three 1-digit numbers.</p>

Skill: Add 1-digit and 2-digit numbers to 100

Year: 2/3



$$38 + 5 = 43$$



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

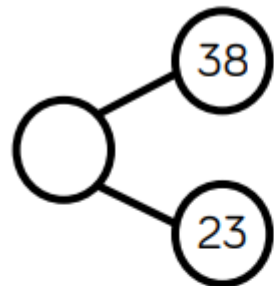
When adding single digits to a two-digit number, children should be encouraged to count on from the larger number.

They should also apply their knowledge of number bonds to add more efficiently e.g. $8 + 5 = 13$ so $38 + 5 = 43$.

Hundred squares and straws can support children to find the number bond to 10.

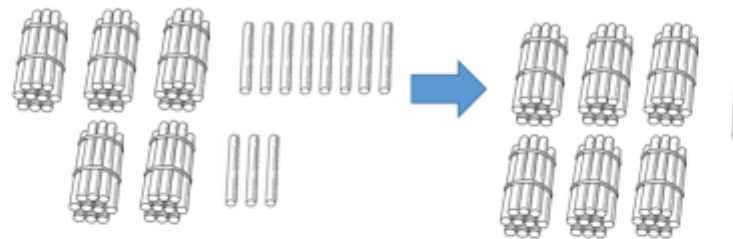
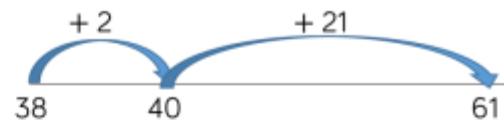
Skill: Add two 2-digit numbers to 100

Year: 2/3



?

38	23
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$$38 + 23 = 61$$

Tens	Ones

$$\begin{array}{r} 38 \\ + 23 \\ \hline 61 \\ 1 \end{array}$$

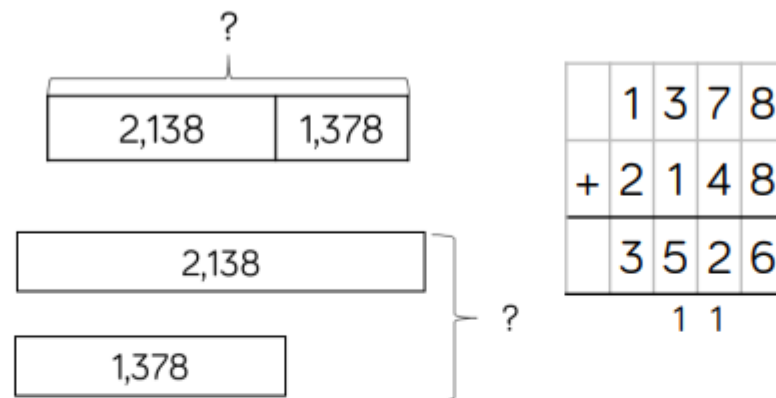
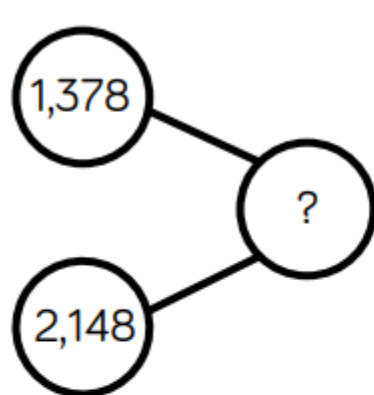
Tens	Ones
10 10 10	1 1 1 1
10 10	1 1 1 1
10	1 1 1

Children can use a blank number line and other representations to count on to find the total. Encourage them to jump to multiples of 10 to become more efficient. From Year 3, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.

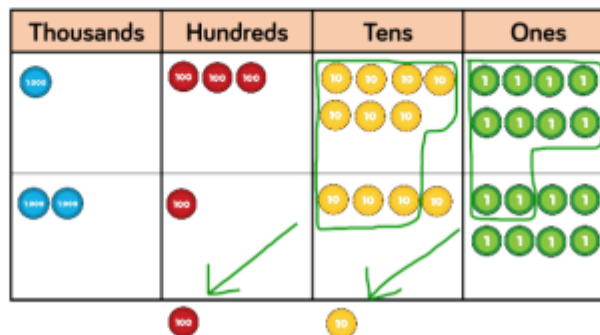
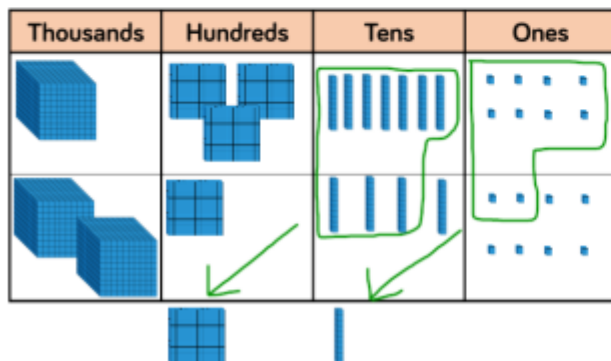
Skill: Add numbers with up to 3 digits	Year: 3																		
<div><div><div><div>?</div><div>265</div><div>164</div></div><div><div>?</div><div>265</div><div>164</div></div><div><div>265</div><div>164</div></div><div><div>265</div><div>164</div></div></div><div><div>265 + 164 = 429</div></div><div><div><table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td><div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div></div></td></tr><tr><td><div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div></div></td></tr></table><div><div></div></div></div><div><div><table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td><div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div></div></td></tr><tr><td><div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div></div></td></tr></table><div><div></div></div></div></div></div></div>	Hundreds	Tens	Ones	<div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div></div>	Hundreds	Tens	Ones	<div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div></div>	<div><p>Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 3 digits.</p><p>Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.</p><p>Plain counters on a place value grid can also be used to support learning.</p></div>
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Skill: Add numbers with up to 4 digits

Year: 4



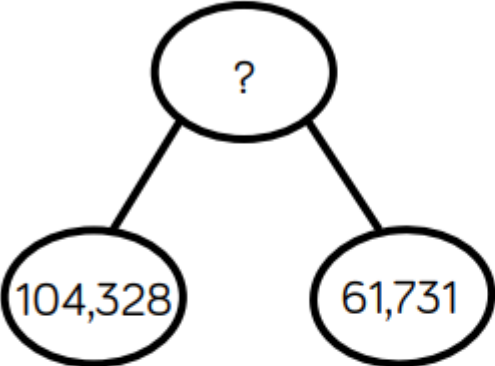
$$1,378 + 2,148 = 3,526$$



Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

Skill: Add numbers with more than 4 digits	Year: 5/6																						
<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;"> <p>?</p> <table border="1" style="margin: 0 auto; border-collapse: collapse;"> <tr> <td style="padding: 5px;">104,328</td> <td style="padding: 5px;">61,731</td> </tr> </table> </div> </div> <div style="margin-top: 20px; text-align: center;"> <table border="1" style="margin: 0 auto; border-collapse: collapse;"> <tr> <td style="padding: 5px;">104,328</td> </tr> <tr> <td style="padding: 5px;">61,731</td> </tr> </table> <p style="font-size: 2em; margin-top: 10px;">}</p> <p style="margin-top: 10px;">?</p> </div> <div style="margin-top: 20px; text-align: center; border: 1px solid black; padding: 10px; border-radius: 10px;"> <p style="font-size: 1.2em; margin: 0;">$104,328 + 61,731 = 166,059$</p> </div> <div style="margin-top: 20px;"> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #f4cccc;"> <th style="padding: 5px;">HTh</th> </tr> <tr> <td style="padding: 5px;">100,000</td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #ccccff;"> <th style="padding: 5px;">TTh</th> </tr> <tr> <td style="padding: 5px;"></td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #cfe2f3;"> <th style="padding: 5px;">Th</th> </tr> <tr> <td style="padding: 5px;">1,000 1,000 1,000 1,000</td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #d9ead3;"> <th style="padding: 5px;">H</th> </tr> <tr> <td style="padding: 5px;">100 100 100</td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #fff2cc;"> <th style="padding: 5px;">T</th> </tr> <tr> <td style="padding: 5px;">10 10</td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr style="background-color: #f4cccc;"> <th style="padding: 5px;">O</th> </tr> <tr> <td style="padding: 5px;">1 1 1 1 1 1 1 1</td> </tr> </table> <table border="1" style="display: inline-table; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 5px;"></td> <td style="padding: 5px;">10,000 10,000 10,000 10,000 10,000 10,000</td> <td style="padding: 5px;">1,000</td> <td style="padding: 5px;">100 100 100 100 100 100 100</td> <td style="padding: 5px;">10 10 10</td> <td style="padding: 5px;">1</td> </tr> </table> </div>	104,328	61,731	104,328	61,731	HTh	100,000	TTh		Th	1,000 1,000 1,000 1,000	H	100 100 100	T	10 10	O	1 1 1 1 1 1 1 1		10,000 10,000 10,000 10,000 10,000 10,000	1,000	100 100 100 100 100 100 100	10 10 10	1	<p>Place value counters or plain counters on a place value grid are the most effective concrete resources when adding numbers with more than 4 digits.</p> <p>At this stage, children should be encouraged to work in the abstract, using the column method to add larger numbers efficiently.</p>
104,328	61,731																						
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Skill: Add with up to 3 decimal places	Year: 5
<div data-bbox="297 363 728 730"> </div> <div data-bbox="779 363 1220 778"> </div> <div data-bbox="1317 432 1518 722"> $\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array}$ </div> <div data-bbox="645 794 1240 898"> $3.65 + 2.41 = 6.06$ </div> <div data-bbox="353 959 947 1289"> </div> <div data-bbox="1059 954 1462 1281"> </div>	<p>Place value counters and plain counters on a place value grid are the most effective manipulatives when adding decimals with 1, 2 and then 3 decimal places.</p> <p>Ensure children have experience of adding decimals with a variety of decimal places. This includes putting this into context when adding money and other measures.</p>

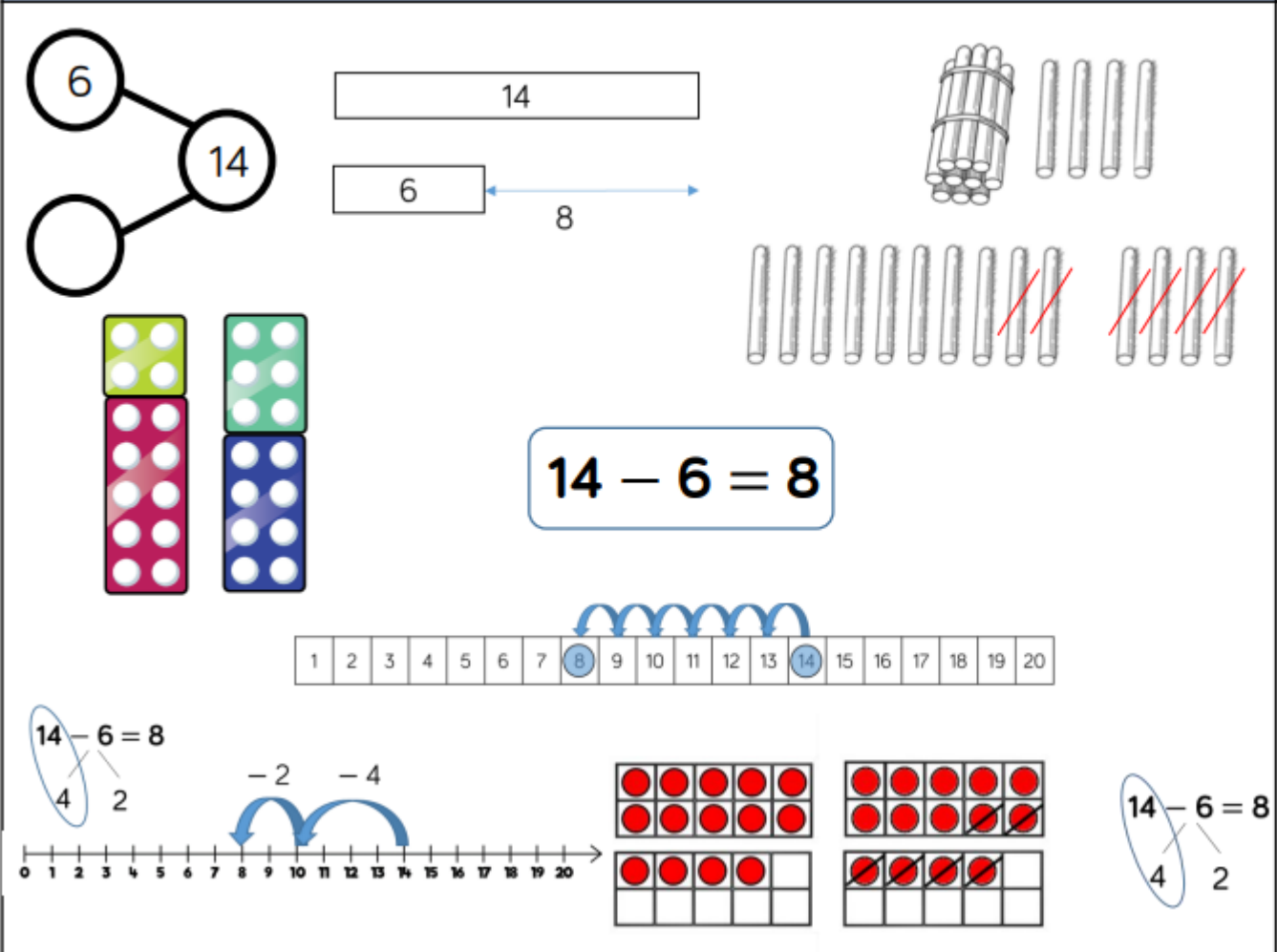
Subtraction

Skill	Year	Representations and models	
Subtract two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes	Ten frames (within 10) Bead strings (10) Number tracks
Subtract 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20)	Bead string (20) Number tracks Number lines (labelled) Straws
Subtract 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled)	Number lines (blank) Straws Hundred square
Subtract two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws	Base 10 Place value counters

Progression of Calculation in Mathematics Policy

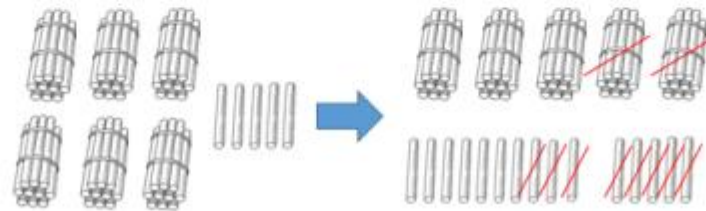
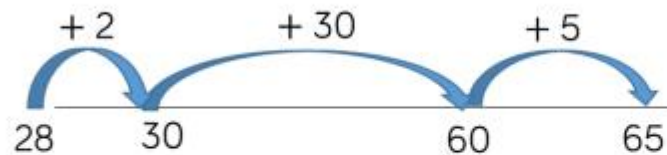
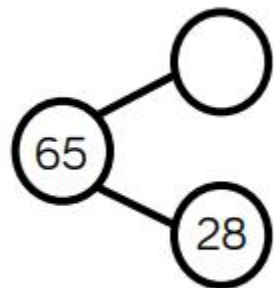
Skill	Year	Representations and models	
Subtract with up to 3-digits	3	Part-whole model Bar model	Base 10 Place value counters Column subtraction
Subtract with up to 4-digits	4	Part-whole model Bar model	Base 10 Place value counters Column subtraction
Subtract with more than 4 digits	5	Part-whole model Bar model	Place value counters Column subtraction
Subtract with up to 3 decimal places	5	Part-whole model Bar model	Place value counters Column subtraction

Skill: Subtract 1-digit numbers within 10	Year: 1
<p>$7 - 3 = 4$</p>	<p>Part-whole models, bar models, ten frames and number shapes support partitioning.</p> <p>Ten frames, number tracks, single bar models and bead strings support reduction.</p> <p>Cubes and bar models with two bars can support finding the difference.</p>

Skill: Subtract 1 and 2-digit numbers to 20	Year: 1/2
	<p>In Year 1, subtracting one-digit numbers that cross 10, is done by counting back, using objects, number tracks and number lines. From Year 2, children should be encouraged to find the number bond to 10 when partitioning the subtracted number. Ten frames, number shapes and number lines are particularly useful for this.</p>

Skill: Subtract 1 and 2-digit numbers to 100

Year: 2/3



65	
?	28

$$65 - 28 = 37$$

Tens	Ones

$$\begin{array}{r} 5 1 \\ 65 \\ - 28 \\ \hline 37 \end{array}$$

Tens	Ones

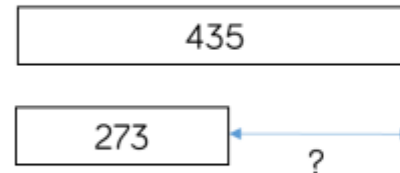
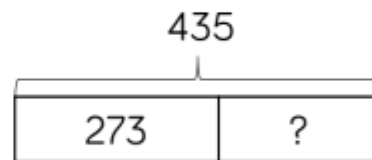
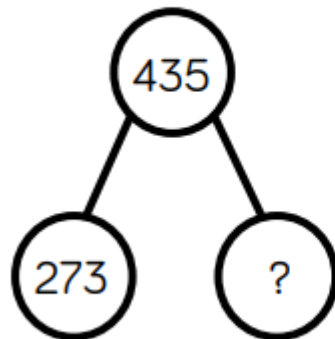
Children can also use a blank number line to count back to find the difference.

Encourage them to jump to multiples of 10 to become more efficient.

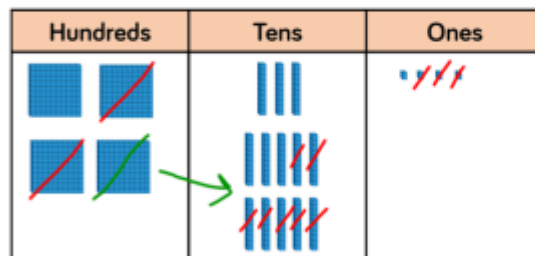
From Year 3, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.

Skill: Subtract numbers with up to 3 digits

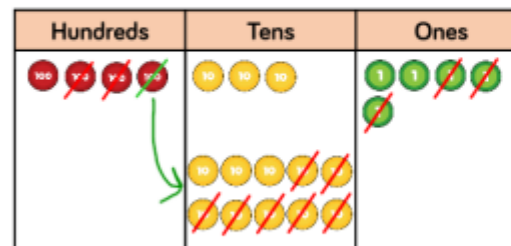
Year: 3



$$435 - 273 = 262$$



$$\begin{array}{r} 3 1 \\ 435 \\ - 273 \\ \hline 262 \end{array}$$



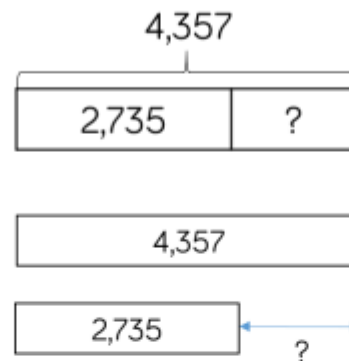
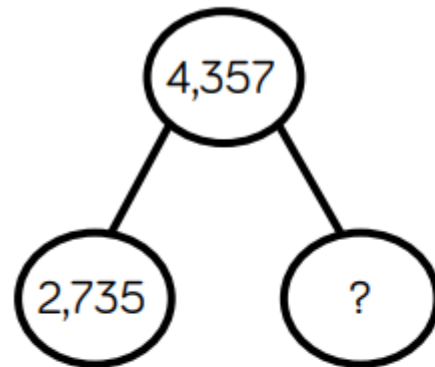
Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

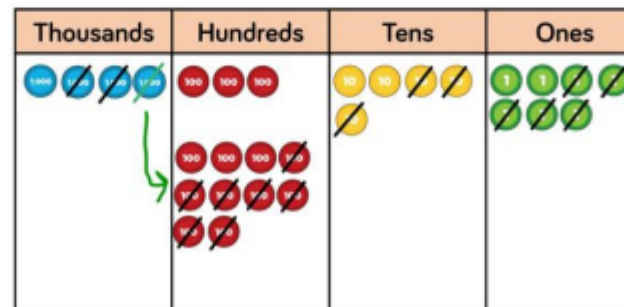
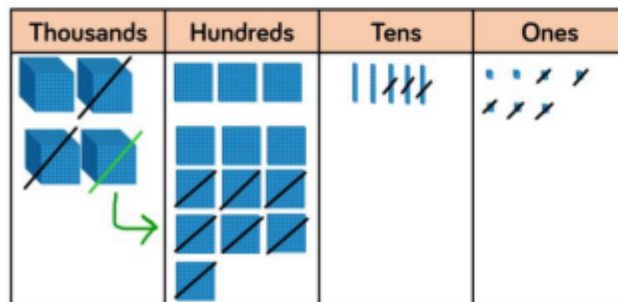
Skill: Subtract numbers with up to 4 digits

Year: 4



$$\begin{array}{r}
 \begin{smallmatrix} 3 & 1 \\ \cancel{4} & \cancel{3} \end{smallmatrix} 57 \\
 - 2735 \\
 \hline
 1622
 \end{array}$$

$$4,357 - 2,735 = 1,622$$



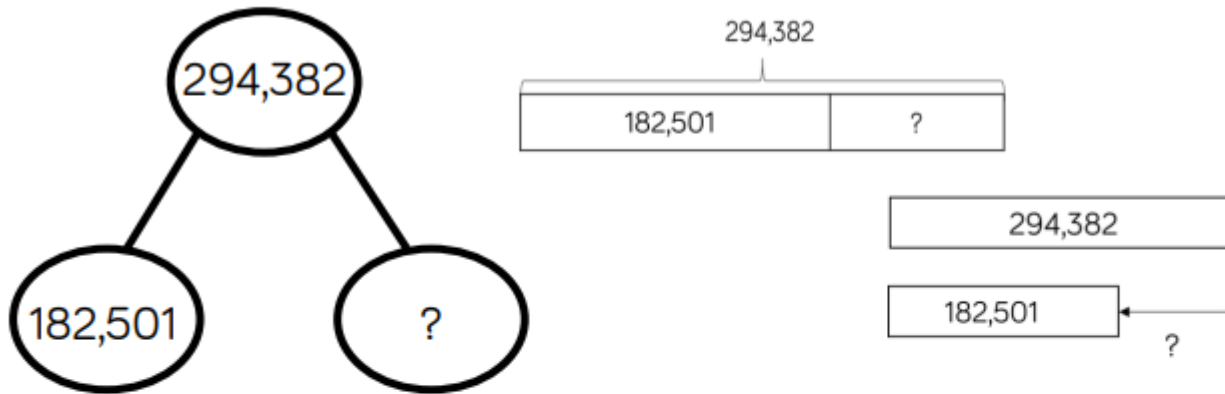
Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.







Plain counters on a place value grid can also be used to support learning.

Skill: Subtract numbers with more than 4 digits

Year: 5/6



$$294,382 - 182,501 = 111,881$$

HTh	TTh	Th	H	T	O
					

	2	9	3	13	8	2
-	1	8	2	5	0	1
	1	1	1	8	8	1

Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.

At this stage, children should be encouraged to work in the abstract, using column method to subtract larger numbers efficiently.

Skill: Subtract with up to 3 decimal places	Year: 5/6
<div data-bbox="295 363 725 730"> </div> <div data-bbox="779 363 1214 785"> </div> <div data-bbox="1285 389 1469 644"> </div> <div data-bbox="645 794 1238 901"> $5.43 - 2.7 = 2.73$ </div> <div data-bbox="315 963 978 1289"> </div> <div data-bbox="1048 948 1541 1305"> </div>	<p>Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.</p> <p>Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.</p>

Multiplication

Skill	Year	Representations and models	
Solve one-step problems with multiplication	1/2	Bar model Number shapes Counters	Ten frames Bead strings Number lines
Multiply 2-digit by 1-digit numbers	3/4	Place value counters Base 10	Expanded written method Short written method
Multiply 3-digit by 1-digit numbers	4	Place value counters Base 10	Short written method
Multiply 4-digit by 1-digit numbers	5	Place value counters	Short written method











Progression of Calculation in Mathematics Policy

Skill	Year	Representations and models	
Multiply 2-digit by 2-digit numbers	5	Place value counters Base 10	Short written method Grid method
Multiply 2-digit by 3-digit numbers	5	Place value counters	Short written method Grid method
Multiply 2-digit by 4-digit numbers	5/6	Formal written method	

Skill: Solve 1-step problems using multiplication	Year: 1/2
<div data-bbox="353 352 616 719"> </div> <div data-bbox="689 352 1503 667"> </div> <div data-bbox="607 703 1312 858"> <p>One bag holds 5 apples. How many apples do 4 bags hold?</p> </div> <div data-bbox="360 890 741 1222"> </div> <div data-bbox="837 874 1447 1246"> </div> <div data-bbox="1144 1066 1518 1246"> $5 + 5 + 5 + 5 = 20$ $4 \times 5 = 20$ $5 \times 4 = 20$ </div>	<p>Children represent multiplication as repeated addition in many different ways.</p> <p>In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record multiplication formally.</p> <p>In Year 2, children are introduced to the multiplication symbol.</p>

Skill: Multiply 2-digit numbers by 1-digit numbers


Year: 3/4

Hundreds	Tens	Ones
		
		
		
		
		

	H	T	O		
		3	4		
x			5		
		2	0	(5 × 4)	
+	1	5	0	(5 × 30)	
	1	7	0		

$$34 \times 5 = 170$$

	H	T	O	
		3	4	
×			5	
	1	7	0	
	1	2		

Hundreds	Tens	Ones
		
		
		
		
		
		

Informal methods and the expanded method are used in Year 3 before moving on to the short multiplication method in Year 4.

Place value counter should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.

Skill: Multiply 3-digit numbers by 1-digit numbers

Year: 4

	H	T	O
	2	4	5
x			4
	9	8	0
	1	2	

$$245 \times 4 = 980$$

When moving to 3-digit by 1-digit multiplication, encourage children to move towards the short, formal written method.

Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in the questions and move children away from resources when multiplying larger numbers.

Skill: Multiply 4-digit numbers by 1-digit numbers

Year: 5

$$1,826 \times 3 = 5,478$$

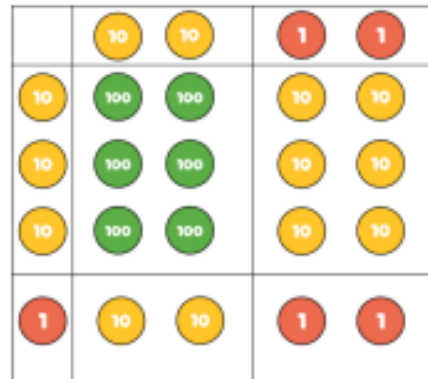
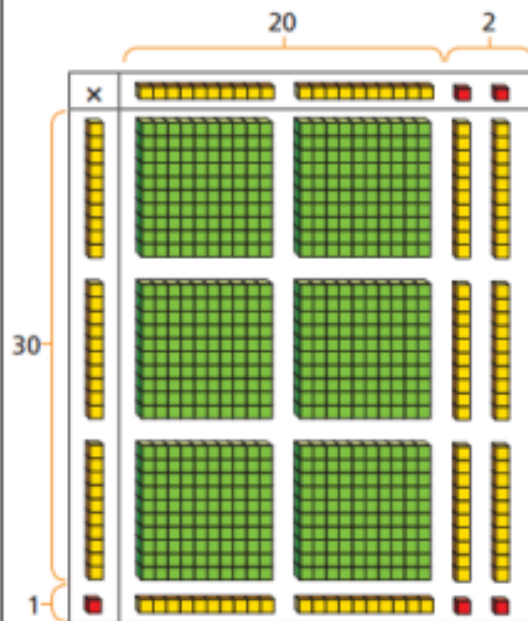
	Th	H	T	O
	1	8	2	6
×				3
	5	4	7	8
	2		1	

When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method.

If children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so children can focus on the use of the written method.

Skill: Multiply 2-digit numbers by 2-digit numbers

Year: 5



\times	20	2
30	600	60
1	20	2

	H	T	O
		2	2
\times		3	1
		2	2
	6	6	0
	6	8	2

$$22 \times 31 = 682$$

When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10.

The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.

Skill: Multiply 3-digit numbers by 2-digit numbers

Year: 5

100100

101010

1111

10

10001000

100100100

100100100

1

100100

101010

1111

10

10001000

100100100

100100100

100100100

100100100

100100100

101010

101010

1111

Th	H	T	O
	2	3	4
x		3	2
	4	6	8
17	10	2	0
7	4	8	8

234 × 32 = 7,488

x	200	30	4
30	6,000	900	120
2	400	60	8

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.

Children should now move towards the formal written method, seeing the links with the grid method.

Skill: Multiply 4-digit numbers by 2-digit numbers	Year: 5/6																																								
<table><tr><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td>2</td><td>7</td><td>3</td><td>9</td></tr><tr><td>×</td><td></td><td></td><td>2</td><td>8</td></tr><tr><td>2</td><td>1</td><td>9</td><td>1</td><td>2</td></tr><tr><td>2</td><td>5</td><td>3</td><td>7</td><td></td></tr><tr><td>5</td><td>4</td><td>7</td><td>8</td><td>0</td></tr><tr><td>1</td><td></td><td>1</td><td></td><td></td></tr><tr><td>7</td><td>6</td><td>6</td><td>9</td><td>2</td></tr></table> <p style="text-align: center;">1</p> <div>2,739 × 28 = 76,692</div>	TTh	Th	H	T	O		2	7	3	9	×			2	8	2	1	9	1	2	2	5	3	7		5	4	7	8	0	1		1			7	6	6	9	2	<p>When multiplying 4-digits by 2-digits, children should be confident in using the formal written method.</p> <p>If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.</p> <p>Consider where exchanged digits are placed and make sure this is consistent.</p>
TTh	Th	H	T	O																																					
	2	7	3	9																																					
×			2	8																																					
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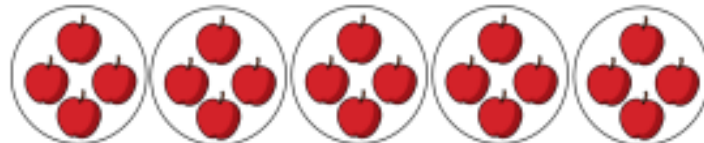
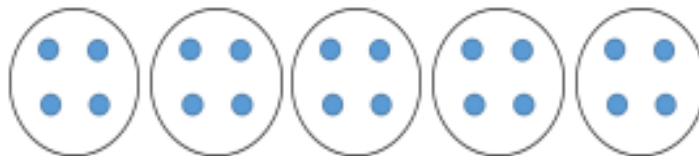
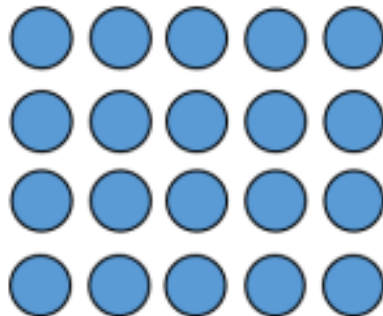
Division

Skill	Year	Representations and models
Solve one-step problems with division (sharing)	1/2	Bar model Real life objects Arrays Counters
Solve one-step problems with division (grouping)	1/2	Real life objects Number shapes Bead strings Ten frames Number lines Arrays Counters
Divide 2-digits by 1-digit (no exchange sharing)	3	Straws Base 10 Bar model Place value counters Part-whole model
Divide 2-digits by 1-digit (sharing with exchange)	3	Straws Base 10 Bar model Place value counters Part-whole model





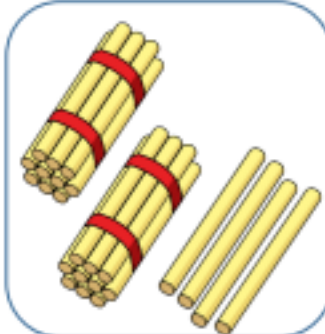
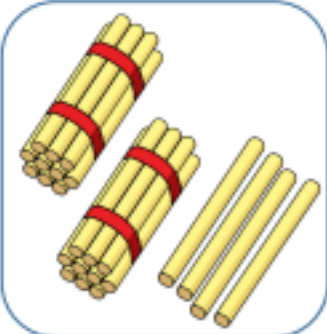
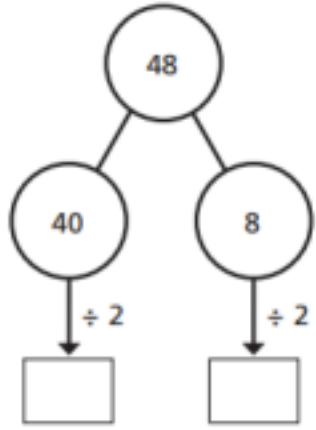
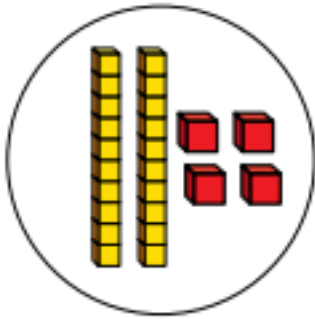
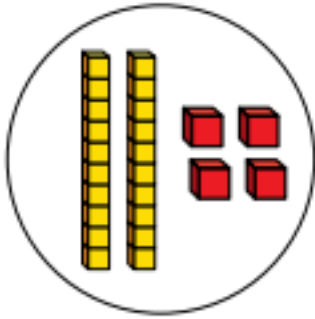








Skill	Year	Representations and models	
Divide 2-digits by 1-digit (sharing with remainders)	3/4	Straws Base 10 Bar model	Place value counters Part-whole model
Divide 2-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division
Divide 3-digits by 1-digit (sharing with exchange)	4	Base 10 Bar model	Place value counters Part-whole model
Divide 3-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division

Progression of Calculation in Mathematics Policy

Skill	Year	Representations and models	
Divide 4-digits by 1-digit (grouping)	5	Place value counters Counters	Place value grid Written short division
Divide multi-digits by 2-digits (short division)	6	Written short division	List of multiples
Divide multi-digits by 2-digits (long division)	6	Written long division	List of multiples

Skill: Solve 1-step problems using multiplication (sharing)	Year: 1/2										
<div><table data-bbox="1055 389 1538 612"><tr><td colspan="5">20</td></tr><tr><td>?</td><td>?</td><td>?</td><td>?</td><td>?</td></tr></table></div> <div><div>There are 20 apples altogether. They are shared equally between 5 bags. How many apples are in each bag?</div><div>$20 \div 5 = 4$</div></div>	20					?	?	?	?	?	<p>Children solve problems by sharing amounts into equal groups.</p> <p>In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division formally.</p> <p>In Year 2, children are introduced to the division symbol.</p>
20											
?	?	?	?	?							

Skill: Solve 1-step problems using division (grouping)	Year: 1/2
<div data-bbox="297 371 589 762"> </div> <div data-bbox="651 376 1507 715"> </div> <div data-bbox="584 730 1323 916"> <p>There are 20 apples altogether. They are put in bags of 5. How many bags are there?</p> </div> <div data-bbox="309 943 712 1289"> </div> <div data-bbox="808 922 1451 1321"> </div> <div data-bbox="1198 1185 1422 1233"> $20 \div 5 = 4$ </div>	<p>Children solve problems by grouping and counting the number of groups. Grouping encourages children to count in multiples and links to repeated subtraction on a number line. They can use concrete representations in fixed groups such as number shapes which helps to show the link between multiplication and division.</p>

Skill: Divide 2-digits by 1-digit (sharing with no exchange)	Year: 3						
<div data-bbox="313 414 878 654"> <table border="1"> <thead> <tr> <th>Tens</th><th>Ones</th></tr> </thead> <tbody> <tr> <td></td><td></td></tr> <tr> <td></td><td></td></tr> </tbody> </table> </div> <div data-bbox="896 375 1220 710">  </div> <div data-bbox="1243 375 1568 710">  </div> <div data-bbox="324 821 638 1252">  </div> <div data-bbox="712 810 1182 922"> <div> $48 \div 2 = 24$ </div> </div> <div data-bbox="824 970 1137 1289">  </div> <div data-bbox="1176 970 1489 1289">  </div>	Tens	Ones					<p>When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.</p> <p>Straws, Base 10 and place value counters can all be used to share numbers into equal groups.</p> <p>Part-whole models can provide children with a clear written method that matches the concrete representation.</p>
Tens	Ones						
							
							

Skill: Divide 2-digits by 1-digit (sharing with exchange)

Year: 3/4

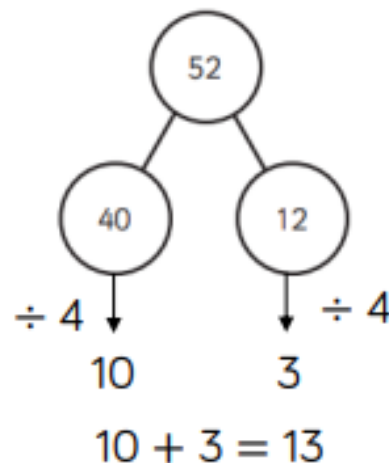


Tens	Ones

52

?	?	?	?
---	---	---	---

$$52 \div 4 = 13$$



A diagram showing the division of 52 into 40 and 12, then dividing each by 4 to get 10 and 3, and finally adding them to get 13. It includes a place value grid with 40 tens rods and 20 ones units, which are then shared into 4 groups of 10 tens and 3 ones each.

Tens	Ones

When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones.

Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows.

Flexible partitioning in a part-whole model supports this method.

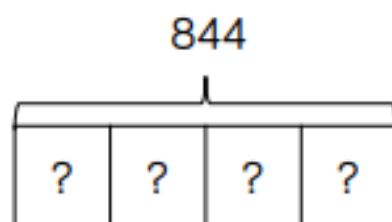
Skill: Divide 2-digits by 1-digit (sharing with remainders)	Year: 3/4																			
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<div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></div></div><div><table><tr><th>Tens</th><th>Ones</th></tr><tr><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td></tr><tr><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td></tr><tr><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td></tr><tr><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td></tr></table></div><div><div>1</div></div></div> <div><p>When dividing numbers with remainders, children can use Base 10 and place value counters to exchange one ten for ten ones.</p><p>Starting with the equipment outside the place value grid will highlight remainders, as they will be left outside the grid once the equal groups have been made.</p><p>Flexible partitioning in a part-whole model supports this method.</p></div>	Tens	Ones	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	Tens	Ones	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>
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Skill: Divide 2-digits by 1-digit (grouping)	Year: 5																		
<div><table><tr><th>Tens</th><th>Ones</th></tr><tr><td><div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div></td><td><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div></td></tr></table><div><table><tr><td></td><td></td><td>1</td><td>3</td><td></td></tr><tr><td></td><td>4</td><td>5</td><td>12</td><td></td></tr></table></div><div><table><tr><th>Tens</th><th>Ones</th></tr><tr><td><div><div></div><div></div><div></div><div></div><div></div></div></td><td><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></td></tr></table><div><div>52 ÷ 4 = 13</div></div></div></div>	Tens	Ones	<div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div>	<div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div>			1	3			4	5	12		Tens	Ones	<div><div></div><div></div><div></div><div></div><div></div></div>	<div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div>	<p>When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.</p> <p>Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'</p> <p>Remainders can also be seen as they are left ungrouped.</p>
Tens	Ones																		
<div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div>	<div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div>																		
		1	3																
	4	5	12																
Tens	Ones																		
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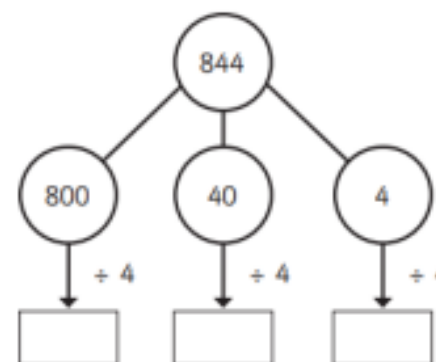
Skill: Divide 3-digits by 1-digit (sharing)

Year: 4

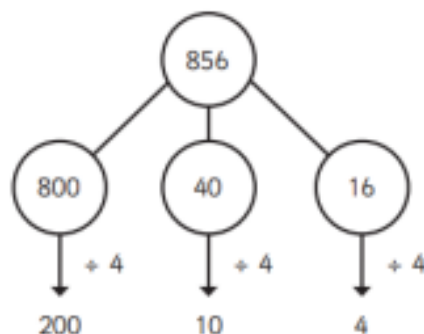
$$844 \div 4 = 211$$



H	T	O
100 100	10	1
100 100	10	1
100 100	10	1
100 100	10	1



$$856 \div 4 = 214$$



Hundreds	Tens	Ones
100 100	10	1 1 1 1
100 100	10	1 1 1 1
100 100	10	1 1 1 1
100 100	10	1 1 1 1

Children can continue to use place value counters to share 3-digit numbers into equal groups. Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows. This method can also help to highlight remainders. Flexible partitioning in a part-whole model supports this method.

Skill: Divide 3-digits by 1-digit (grouping)

Year: 5

Hundreds	Tens	Ones
100 100 100 100	10 10 10 10	1 1 1 1
100 100 100 100	10	1 1 1 1 1 1 1 1 1 1

		2	1	4
	4	8	5	16

$$856 \div 4 = 214$$











































Hundreds	Tens	Ones
● ● ● ●	● ● ● ●	● ● ● ●
● ● ● ●	●	● ● ● ● ● ● ● ● ● ●

Children can continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number.

Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.

Skill: Divide 4-digits by 1-digit (grouping)

Year: 5

Th	H	T	O
 	 	 	 
 	 	 →  	 
 	 →  	 	 
 		 	 
		 	 
		 	 
		 	

	4	2	6	6
2	8	5	13	12

$$8,532 \div 2 = 4,266$$

Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method.

Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.

Skill: Divide multi digits by 2-digits (short division)	Year: 6																														
<table><tr><td></td><td></td><td>0</td><td>3</td><td>6</td></tr><tr><td></td><td>12</td><td>4</td><td>⁴3</td><td>⁷2</td></tr></table> <div>432 ÷ 12 = 36</div> <table><tr><td></td><td>0</td><td>4</td><td>8</td><td>9</td></tr><tr><td>15</td><td>7</td><td>⁷3</td><td>¹³3</td><td>¹³5</td></tr></table> <table><tr><td>15</td><td>30</td><td>45</td><td>60</td><td>75</td><td>90</td><td>105</td><td>120</td><td>135</td><td>150</td></tr></table>			0	3	6		12	4	⁴ 3	⁷ 2		0	4	8	9	15	7	⁷ 3	¹³ 3	¹³ 5	15	30	45	60	75	90	105	120	135	150	<p>When children begin to divide up to 4-digits by 2-digits, written methods become the most accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be rounded as appropriate.</p>
		0	3	6																											
	12	4	⁴ 3	⁷ 2																											
	0	4	8	9																											
15	7	⁷ 3	¹³ 3	¹³ 5																											
15	30	45	60	75	90	105	120	135	150																						

Skill: Divide multi-digits by 2-digits (long division)

Year: 6

		0	3	6
1	2	4	3	2
	-	3	6	0
			7	2
	-		7	2
				0

(x30) $12 \times 1 = 12$
 $12 \times 2 = 24$
 $12 \times 3 = 36$
 $12 \times 4 = 48$
 $12 \times 5 = 60$
 (x6) $12 \times 6 = 72$
 $12 \times 7 = 84$
 $12 \times 8 = 96$
 $12 \times 9 = 108$
 $12 \times 10 = 120$

$$432 \div 12 = 36$$

$$7,335 \div 15 = 489$$

	0	4	8	9
15	7	3	3	5
-	6	0	0	0
	1	3	3	5
-	1	2	0	0
		1	3	5
-		1	3	5
				0

(x400) $1 \times 15 = 15$
 $2 \times 15 = 30$
 $3 \times 15 = 45$
 (x80) $4 \times 15 = 60$
 $5 \times 15 = 75$
 (x9) $10 \times 15 = 150$

Children can also divide by 2-digit numbers using long division.

Children can write out multiples to support their calculations with larger remainders.

Children will also solve problems with remainders where the quotient can be rounded as appropriate.

Skill: Divide multi digits by 2-digits (long division)

Year: 6

$$372 \div 15 = 24 \text{ r}12$$

			2	4	r	1	2
1	5	3	7	2			
	–	3	0	0			
			7	2			
	–		6	0			
			1	2			

$1 \times 15 = 15$
 $2 \times 15 = 30$
 $3 \times 15 = 45$
 $4 \times 15 = 60$
 $5 \times 15 = 75$
 $10 \times 15 = 150$

			2	4	$\frac{4}{5}$
1	5	3	7	2	
	–	3	0	0	
			7	2	
	–		6	0	
			1	2	

$$372 \div 15 = 24 \frac{4}{5}$$

When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction. This will depend on the context of the question.

Children can also answer questions where the quotient needs to be rounded according to the context.

Glossary

Addend - A number to be added to another.

Aggregation - combining two or more quantities or measures to find a total.

Augmentation - increasing a quantity or measure by another quantity.

Commutative - numbers can be added in any order.

Complement - in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

Difference - the numerical difference between two numbers is found by comparing the quantity in each group.

Exchange - Change a number or expression for another of an equal value.

Minuend - A quantity or number from which another is subtracted.

Partitioning - Splitting a number into its component parts.

Reduction - Subtraction as take away.

Subitise - Instantly recognise the number of objects in a small group without needing to count.

Subtrahend - A number to be subtracted from another.

Sum - The result of an addition.

Total - The aggregate or the sum found by addition.

Array – An ordered collection of counters, cubes or other item in rows and columns.

Commutative – Numbers can be multiplied in any order.

Dividend – In division, the number that is divided.

Divisor – In division, the number by which another is divided.

Exchange – Change a number or expression for another of an equal value.

Factor – A number that multiplies with another to make a product.

Multiplicand – In multiplication, a number to be multiplied by another.

Partitioning – Splitting a number into its component parts.

Product – The result of multiplying one number by another.

Quotient – The result of a division

Remainder – The amount left over after a division when the divisor is not a factor of the dividend.

Scaling – Enlarging or reducing a number by a given amount, called the scale factor